

## 9-3 Classifying Conic Sections

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

if  $A=0$  or  $C=0 \rightarrow$  parabola

if  $A=C \rightarrow$  circle

if  $A$  and  $C$  have  
the same sign  $\rightarrow$  ellipse

if  $A$  and  $C$  have  
different signs  $\rightarrow$  hyperbola

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Ex 1 Classify the graph of each equation

a.  $x^2 - 3y^2 - 4x + 1 = 0$

**Hyperbola**

b.  $x^2 + y^2 - 10x + 2y + 22 = 0$

**Circle**

c.  $x^2 - 4x - 24y - 4 = 0$

**Parabola**

d.  $2x^2 + 3y^2 - 28x - 12y + 104 = 0$

**ellipse**

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Ex 2 Classify the conic, rewrite in standard form, graph, and find all of the characteristics.

- ellipse

$$9x^2 + 5y^2 + 36x - 30y + 36 = 0$$

$$9(x^2 + 4x + 4) + 5(y^2 - 6y + 9) = -36$$

$$\frac{9(x+2)^2}{45} + \frac{5(y-3)^2}{45} = \frac{-45}{45}$$

$$\frac{(x+2)^2}{5} + \frac{(y-3)^2}{9} = 1$$

Center  $(-2, 3)$

Foci:  $(-2, 1)$  &  $(2, 3)$

$a^2 = 9$

$b^2 = 5$

$c^2 = a^2 - b^2$

$c^2 = 9 - 5$

$c = 2$

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What if we have an  $xy$  term?

Rotates the  
axis



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Homework

p.689

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